

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

**Pearson Edexcel**

**Level 1/Level 2 GCSE (9–1)**

**Tuesday 19 May 2020**

Morning (Time: 1 hour 30 minutes)

Paper Reference **1MA1/1H**

**Mathematics**

**Paper 1 (Non-Calculator)**

**Higher Tier**

**You must have:** Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser. Tracing paper may be used.

Total Marks

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **show all your working**.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- **Calculators may not be used.**



### Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ➔

P62277RA

©2020 Pearson Education Ltd.

1/1/1/1/



P 6 2 2 7 7 R A 0 1 2 0



Pearson

Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

- 1 The first five terms of an arithmetic sequence are

$$1 \xrightarrow{+3} 4 \xrightarrow{+3} 7 \xrightarrow{+3} 10 \xrightarrow{+3} 13 \rightarrow 3n$$

Write down an expression, in terms of  $n$ , for the  $n$ th term of this sequence.

$n$	1	2	3	4	5	
Term	1	4	7	10	13	
$3n$	3	6	9	12	15	
Term - $3n$	-2	-2	-2	-2	-2	$\rightarrow -2 \quad \therefore 3n - 2$

$3n - 2$  ✓✓

(Total for Question 1 is 2 marks)

- 2 Show that

$$2\frac{1}{3} \times 3\frac{3}{4} = 8\frac{3}{4}$$

- 1) Convert mixed number to improper fraction

$$2\frac{1}{3} = \frac{7}{3} \quad \text{and} \quad 3\frac{3}{4} = \frac{15}{4} \quad ✓$$

- 2) multiply improper fraction

$$\begin{aligned}
 2\frac{1}{3} \times 3\frac{3}{4} &= \frac{7}{3} \times \frac{15}{4} = \frac{7 \times 5}{1 \times 4} = \frac{35}{4} = \frac{32}{4} + \frac{3}{4} \quad \begin{array}{l} \swarrow \text{Whole number} \\ \nwarrow \text{fractional part} \end{array} \\
 &= 8 + \frac{3}{4} \\
 &= 8\frac{3}{4} \quad ✓
 \end{aligned}$$

(Total for Question 2 is 3 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

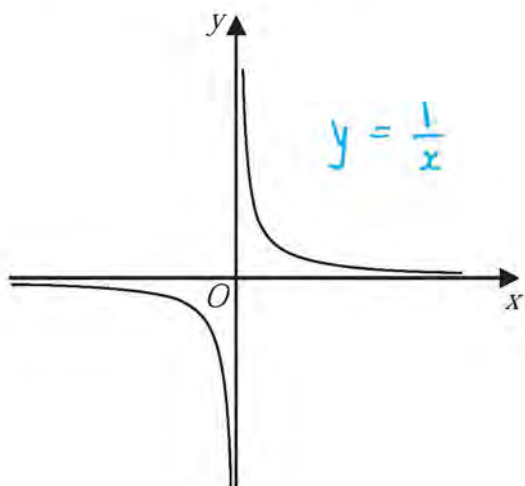


DO NOT WRITE IN THIS AREA

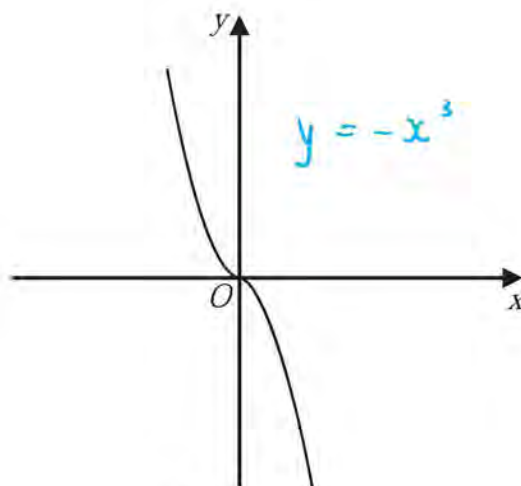
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

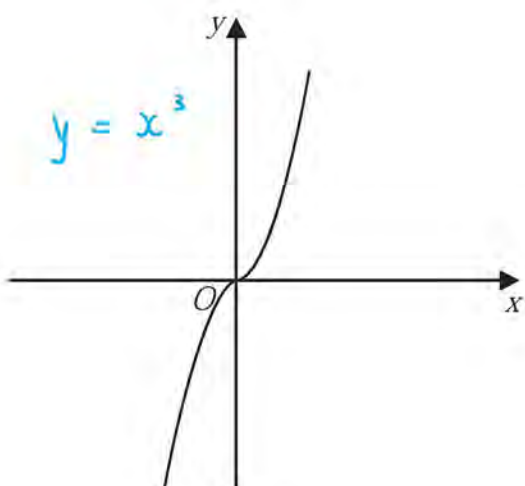
3 The diagram shows four graphs.



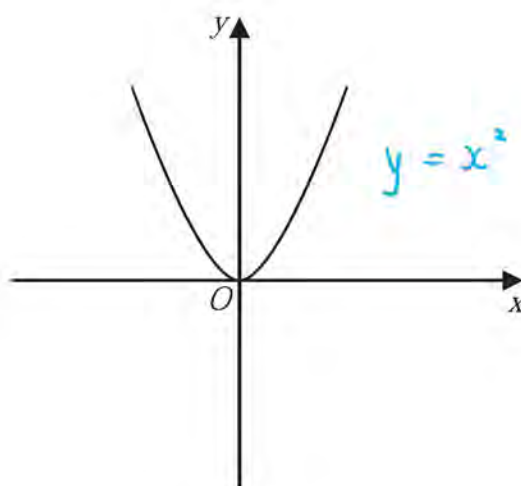
Graph A



Graph B



Graph C

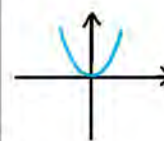
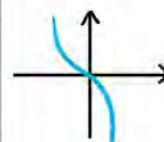
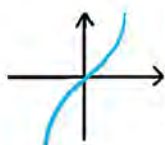


Graph D

Each of the equations in the table is the equation of one of the graphs.

Complete the table.

Equation	Letter of graph
$y = -x^3$	B
$y = x^3$	C
$y = x^2$	D
$y = \frac{1}{x}$	A



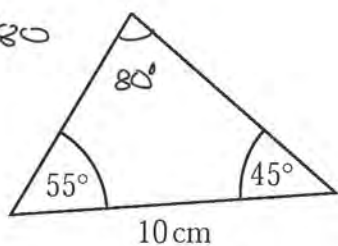
① ①

(Total for Question 3 is 2 marks)

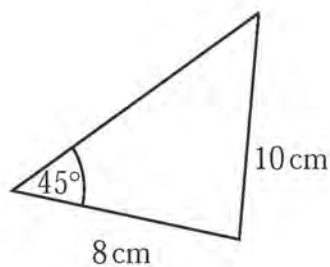


4 The diagram shows four triangles.

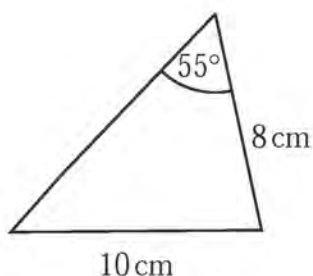
$$180 - 65 - 55 = 80$$



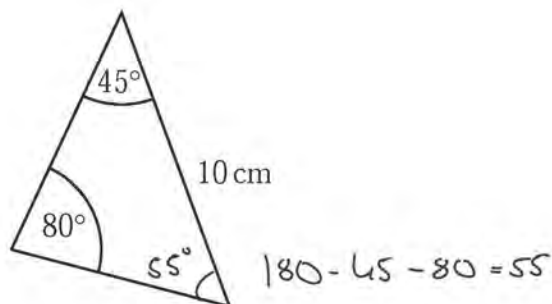
Triangle A



Triangle B



Triangle C



Triangle D

Two of these triangles are congruent.  $\rightarrow$  Same

Write down the letters of these two triangles.

A and D ✓

(Total for Question 4 is 1 mark)

5 Sean pays £10 for 24 chocolate bars.

He sells all 24 chocolate bars for 50p each.

Work out Sean's percentage profit.

$$\text{Revenue (how much he made)} = 24 \times \text{£}0.50 = \text{£}12 \quad \checkmark$$

$$\% \text{ Profit} = \frac{\text{Revenue} - \text{Cost}}{\text{Cost}} \times 100 = \frac{\text{£}12 - \text{£}10}{\text{£}10} \times 100 \quad \checkmark$$

$$= \frac{\text{£}2}{\text{£}10} \times 100 = 0.2 \times 100 = 20\%$$

20 ✓ %

(Total for Question 5 is 3 marks)

DO NOT WRITE IN THIS AREA

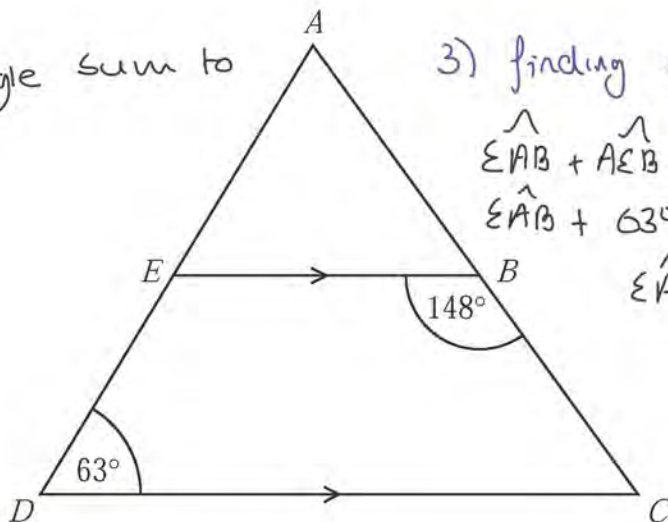
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



6 *ADC* is a triangle.

Angles in a triangle sum to  $180^\circ$  ✓<sub>5</sub>



3) finding  $\hat{\epsilon AB}$

$$\hat{\epsilon AB} + \hat{AEB} + \hat{ABE} = 180^\circ$$

$$\hat{\epsilon AB} + 63^\circ + 32^\circ = 180^\circ$$

$$\hat{\epsilon AB} + 95^\circ = 180^\circ$$

$$\begin{aligned} \hat{\epsilon AB} &= 180^\circ - 95^\circ \\ &= 85^\circ \end{aligned}$$

*AED* and *ABC* are straight lines.

*EB* is parallel to *DC*.

Angle *EBC* =  $148^\circ$

Angle *ADC* =  $63^\circ$

Work out the size of angle *EAB*.

You must give a reason for each stage of your working.

1) finding Angle  $\hat{AEB}$

$\hat{AEB}$  and  $\hat{ADC}$  are corresponding angles (*AE* is on line *AED* and *EB* and *DC* are parallel).

$$\hookrightarrow \hat{AEB} = \hat{ADC} \rightarrow \hat{AEB} = 63^\circ \checkmark_1$$

2) finding Angle  $\hat{ABE}$

Line *ABC* is a straight line, and angles on a line sum to  $180^\circ$  ✓<sub>4</sub>

$$\hat{ABE} + \hat{EBC} = 180^\circ$$

$$\hat{ABE} + 148^\circ = 180^\circ$$

$$\begin{aligned} -148^\circ \quad \swarrow & \quad \searrow \quad -148^\circ \\ \hat{ABE} &= 180^\circ - 148^\circ \\ &= 32^\circ \checkmark_2 \end{aligned}$$

$$\therefore \hat{\epsilon AB} = 85^\circ \checkmark_3$$

(Total for Question 6 is 5 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



7 The table shows information about the heights, in cm, of a group of Year 9 girls.

least height	150 cm
median	165 cm
greatest height	170 cm

$$\text{Range} = 170\text{cm} - 150\text{cm} \\ = 20\text{cm} \checkmark$$

This stem and leaf diagram shows information about the heights, in cm, of a group of 15 Year 9 boys.

15	8 9 9
16	4 5 7 7 8
17	0 3 4 4 7
18	0 2

$$\text{Median position} = \frac{15+1}{2} = 8 \quad \therefore \text{median} = 168\text{cm}$$

Key: 15 | 8 represents 158 cm

$$\text{range} = 182\text{cm} - 156\text{cm} = 26\text{cm}$$

→ Median and range

Compare the distribution of the heights of the girls with the distribution of the heights of the boys.

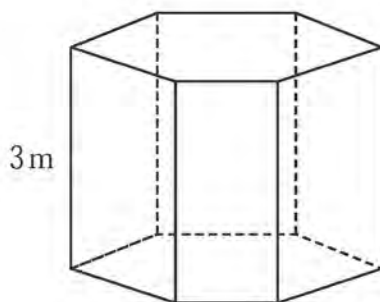
median height for girls is less than median height for boys  
(165 < 168)  $\checkmark$

Range for girls is less than the range for boys (20 < 26)  $\checkmark$

(Total for Question 7 is 3 marks)



- 8 The diagram shows a prism placed on a horizontal floor.

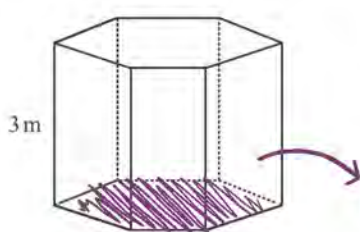


$$\text{pressure} = \frac{\text{force}}{\text{area}}$$

The prism has height 3 m  
The volume of the prism is  $18\text{ m}^3$

The pressure on the floor due to the prism is  $75\text{ newtons/m}^2$

Work out the force exerted by the prism on the floor.



$$\text{pressure} = \frac{\text{force}}{\text{cross-sectional area}}$$

cross-sectional area

Work out cross-sectional area:

$$\text{cross-sectional area} = \frac{\text{volume}}{\text{height}} = \frac{18}{3} = 6\text{ m}^2$$

Work out force:

450 newtons

(Total for Question 8 is 3 marks)

$$\text{pressure} = \frac{\text{force}}{\text{cross-sectional area}}$$

$$75 = \frac{\text{force}}{6}$$

$$\therefore \text{force} = 75 \times 6 = \underline{\underline{450\text{ N}}}$$



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- 9 Write these numbers in order of size. Standard form:  $A \times 10^n$  ( $1 \leq A < 10$ )  
Start with the smallest number.

$$6.72 \times 10^5$$

(3)

$$67.2 \times 10^{-4}$$

↓

$$6.72 \times 10 \times 10^{-4}$$

$$6.72 \times 10^{-3}$$

(2)

$$672 \times 10^4$$

↓

$$6.72 \times 100 \times 10^4$$

$$6.72 \times 10^6$$

(4)

$$0.000672$$

↘

$$6.72 \times 10^{-4}$$

(1)

0.000672     $67.2 \times 10^{-4}$      $6.72 \times 10^5$      $672 \times 10^4$  ✓✓

(Total for Question 9 is 2 marks)





10 Given that  $\frac{a}{b} = \frac{2}{5}$  and  $\frac{b}{c} = \frac{3}{4}$

find  $a:b:c$

$$a:b = 2:5 \quad b:c = 3:4 \quad \checkmark$$

$a:b:c \rightarrow b$  is common

$$b = \text{lcm}(5, 3) = 15$$

$$\begin{array}{ccc} a:b & & b:c \\ \times 3 \swarrow & & \swarrow \times 3 \\ 2:5 & & 3:4 \\ \downarrow \times 3 & & \downarrow \times 3 \\ 6:15 & & 15:20 \end{array} \quad \checkmark$$

$$6:15:20 \quad \checkmark$$

(Total for Question 10 is 3 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



11 (a) Find the value of  $\sqrt[4]{81 \times 10^8}$       $\sqrt{ab} = \sqrt{a} \times \sqrt{b}$       $\sqrt[n]{x^y} = x^{y/n}$

$$\begin{aligned} \sqrt[4]{81 \times 10^8} &= \sqrt[4]{81} \times \sqrt[4]{10^8} \quad \checkmark \\ &= 3 \times 10^{8/4} \quad \downarrow \frac{8}{4} = 2 \\ &= 3 \times 10^2 \\ &= 3 \times 100 = 300 \quad \checkmark \end{aligned}$$

300  
(2)

(b) Find the value of  $64^{-\frac{1}{2}}$       $a^{-b} = \frac{1}{a^b}$       $a^{1/n} = \sqrt[n]{a}$

$$\begin{aligned} 64^{-\frac{1}{2}} &= \frac{1}{64^{\frac{1}{2}}} \\ &= \frac{1}{\sqrt{64}} \quad \checkmark \end{aligned}$$

→ =  $\frac{1}{8}$  ✓

1/8  
(2)

(c) Write  $\frac{3^n}{9^{n-1}}$  as a power of 3

$$\begin{aligned} \frac{3^n}{9^{n-1}} &= \frac{3^n}{(3^2)^{n-1}} = \frac{3^n}{3^{2n-2}} \quad \checkmark \\ &= \frac{3^n}{3^{2n} / 3^2} = \frac{3^n}{1} \times \frac{3^2}{3^{2n}} \\ &= 3^{-n} \times 3^2 \\ &= 3^{2-n} \quad \checkmark \end{aligned}$$

$a^{x-y} = \frac{a^x}{a^y}$       $(a^x)^y = a^{xy}$   
 $\frac{a}{b/c} = \frac{a}{1} \div \frac{b}{c} = \frac{a}{1} \times \frac{c}{b}$       $a^x \times a^y = a^{x+y}$

3^{2-n}  
(2)

(Total for Question 11 is 6 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



12 The table gives information about the weekly wages of 80 people.

Wage (£ $w$ )	Frequency
$200 < w \leq 250$	5
$250 < w \leq 300$	10
$300 < w \leq 350$	20
$350 < w \leq 400$	20
$400 < w \leq 450$	15
$450 < w \leq 500$	10

(a) Complete the cumulative frequency table.

Wage (£ $w$ )	Cumulative frequency
$200 < w \leq 250$	5
$200 < w \leq 300$	15
$200 < w \leq 350$	35
$200 < w \leq 400$	55
$200 < w \leq 450$	70
$200 < w \leq 500$	80

(1)

(b) On the grid opposite, draw a cumulative frequency graph for your completed table.

↳ for grouped data, plot end point of group

(2)

Juan says

"60% of this group of people have a weekly wage of £360 or less."

(c) Is Juan correct?

You must show how you get your answer.

$$\begin{aligned}
 60\% \text{ of group} &= 60\% \text{ of } 80 \text{ people} \\
 &= \frac{60}{100} \times 80 \text{ ppl} \\
 &= \frac{60 \times 80}{100} = 48 \text{ ppl} \checkmark
 \end{aligned}$$

from graph, 60% make  
 $\pounds 380$ .  $\pounds 380 > \pounds 360$   
 $\therefore$  No, he is wrong.  $\checkmark$

(3)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

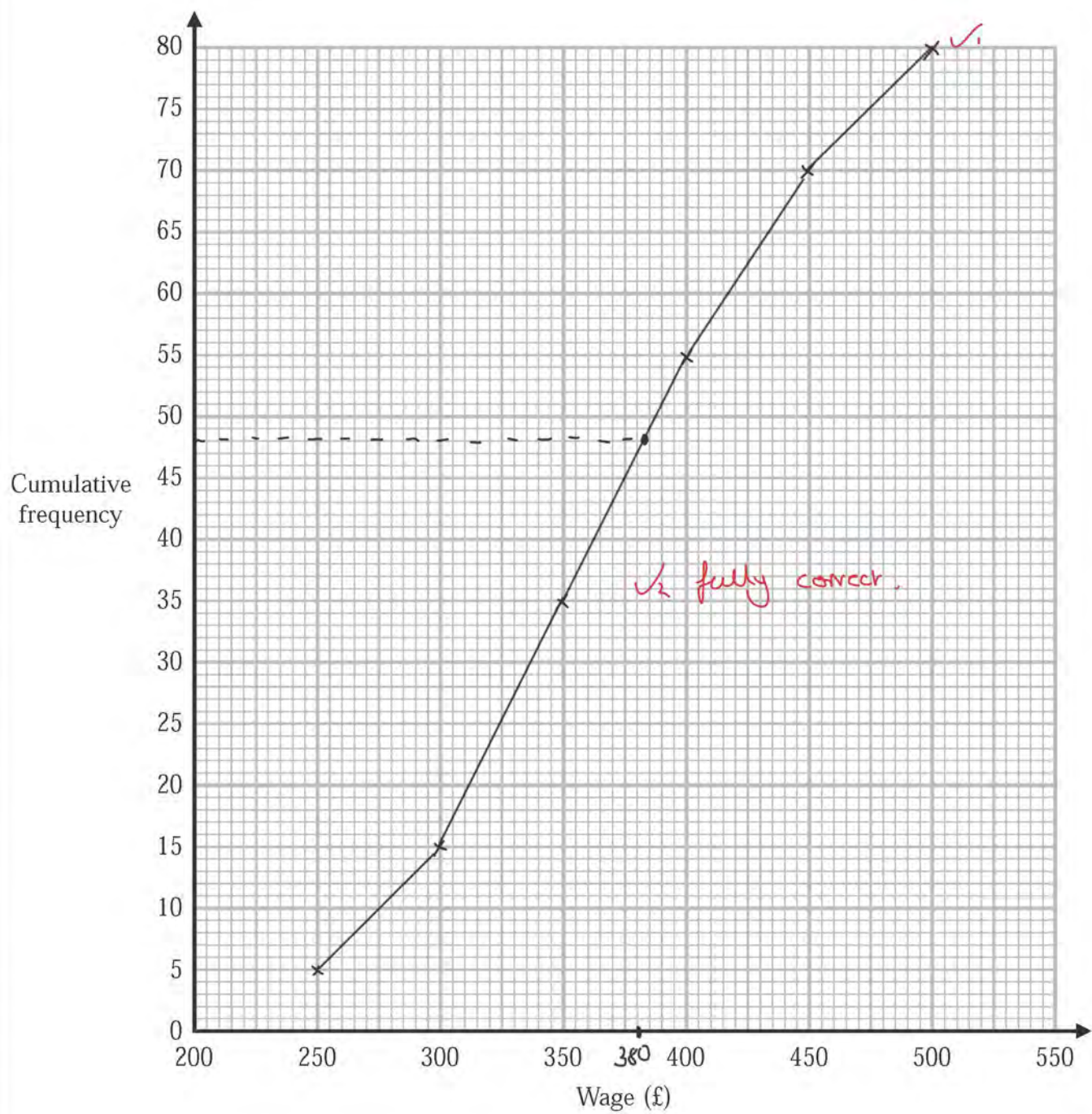
DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



(Total for Question 12 is 6 marks)



13 Liquid A and liquid B are mixed to make liquid C.

Liquid A has a density of  $70 \text{ kg/m}^3$

Liquid A has a mass of  $1400 \text{ kg}$

Liquid B has a density of  $280 \text{ kg/m}^3$

Liquid B has a volume of  $30 \text{ m}^3$

Work out the density of liquid C.

$$\text{density} = \frac{\text{mass}}{\text{Volume}}$$

$$\begin{array}{r} 196 \\ 5 \overline{) 980} \\ \underline{50} \phantom{0} \\ 48 \phantom{0} \\ \underline{45} \phantom{0} \\ 30 \\ \underline{30} \\ 0 \end{array}$$

$$\text{Vol. Liquid A} \rightarrow \text{Vol} = \frac{\text{mass}}{\text{density}} = \frac{1400 \text{ kg}}{70 \text{ kgm}^{-3}} = 20 \text{ m}^3 \checkmark$$

$$\text{mass. Liquid B} \rightarrow \text{mass} = \text{density} \times \text{Vol} = 280 \text{ kgm}^{-3} \times 30 \text{ m}^3 = 8400 \text{ kg}$$

$$\text{Mass. Liquid C} = 1400 \text{ kg} + 8400 \text{ kg} = 9800 \text{ kg}$$

$$\text{Vol. Liquid C} = 20 \text{ m}^3 + 30 \text{ m}^3 = 50 \text{ m}^3$$

$$\text{density. Liquid C} = \frac{9800 \text{ kg} \checkmark}{50 \text{ m}^3} = 196 \text{ kg m}^{-3}$$

$$\underline{\quad 196 \checkmark \quad} \text{ kg/m}^3$$

(Total for Question 13 is 3 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

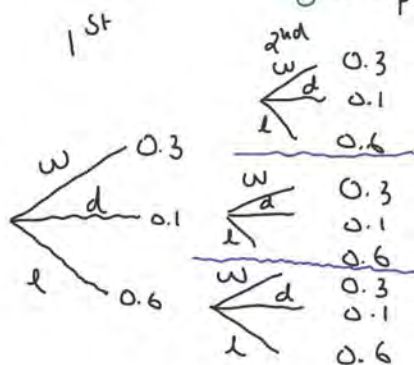
- 14 Sally plays two games against Martin.  
In each game, Sally could win, draw or lose.

In each game they play,  
the probability that Sally will win against Martin is 0.3  $P(L) = 0.6$   
the probability that Sally will draw against Martin is 0.1

Work out the probability that Sally will win exactly one of the two games against Martin

$$P(w) + P(d) + P(l) = 1$$

$$0.3 + 0.1 + P(l) = 1 \rightarrow P(l) + 0.4 = 1 \rightarrow P(l) = 0.6$$



$$P(\text{exactly 1}) = 0.3 \times 0.1 + 0.3 \times 0.6 + 0.1 \times 0.3 + 0.6 \times 0.3$$

$$= 0.03 + 0.18 + 0.03 + 0.18$$

$$= 0.42$$

0.42 ✓

(Total for Question 14 is 3 marks)

- 15 The straight line  $L_1$  has equation  $y = 3x - 4$   
The straight line  $L_2$  is perpendicular to  $L_1$  and passes through the point (9, 5)

Find an equation of line  $L_2$

$$m_{L_1} \times m_{L_2} = -1$$

$$3 \times m_{L_2} = -1$$

$$m_{L_2} = -\frac{1}{3} \checkmark$$

$$y = -\frac{1}{3}x + c$$

at  $x = 9, y = 5$

$$5 = -\frac{1}{3} \times 9 + c$$

$$5 = -3 + c$$

$$5 = -3 + c$$

$$c = 8$$

$$y = -\frac{1}{3}x + 8 \checkmark$$

(Total for Question 15 is 3 marks)



16 Shirley wants to find an estimate for the number of bees in her hive.

On Monday she catches 90 of the bees.  
She puts a mark on each bee and returns them to her hive.

$M = \text{marked}$   
 $T = \text{Total caught}$

On Tuesday she catches 120 of the bees.  
She finds that 20 of these bees have been marked.

(a) Work out an estimate for the total number of bees in her hive.

$$\begin{array}{l}
 M : T \qquad m : t \\
 90 : 120 \qquad 20 : n \\
 \\
 \times n \quad \frac{20}{120} = \frac{90}{n} \quad \downarrow \times n \\
 \frac{20n}{120} = 90 \\
 \\
 20n = 90 \times 120 \\
 n = \frac{90 \times 120}{20} \quad \downarrow \div 20 \\
 n = 90 \times 6 = 540 \quad \checkmark
 \end{array}$$

540  
-----  
(3)

Shirley assumes that none of the marks had rubbed off between Monday and Tuesday.

(b) If Shirley's assumption is wrong, explain what effect this would have on your answer to part (a).

fewer marked bees. This means the answer will be over-estimated. ✓

(1)

(Total for Question 16 is 4 marks)



17 Make  $f$  the subject of the formula  $d = \frac{3(1-f)}{f-4}$

$$\times (f-4) \downarrow \quad \downarrow \times (f-4)$$

$$(f-4)d = 3(1-f) \quad \checkmark_1$$

$$fd - 4d = 3 - 3f$$

$$fd + 3f = 4d + 3 \quad \checkmark_2$$

$$\div (d+3) \downarrow \quad \div (d+3)$$

$$f(d+3) = 4d+3$$

$$f = \frac{4d+3}{d+3}$$

$$f = \frac{4d+3}{d+3} \quad \checkmark_4$$

(Total for Question 17 is 4 marks)

18  $x$  is proportional to  $\sqrt{y}$  where  $y > 0 \rightarrow x = k\sqrt{y} \quad \checkmark_1$

$y$  is increased by 44%  $y_n = y \times 1.44$

Work out the percentage increase in  $x$ .

$$\hookrightarrow x_n = k \times \sqrt{y \times 1.44} \quad \checkmark_2 \quad \sqrt{a \times b} = \sqrt{a} \times \sqrt{b}$$

$$x_n = k \times \sqrt{y} \times \sqrt{1.44}$$

$$x_n = k\sqrt{y} \times 1.2$$

$$x_n = x \times 1.2 \rightarrow 20\% \text{ increase} \quad \checkmark_3$$

..... 20% .....

(Total for Question 18 is 3 marks)





19 f and g are functions such that

$$f(x) = \frac{12}{\sqrt{x}} \quad \text{and} \quad g(x) = 3(2x+1)$$

(a) Find  $g(5)$

↳ Substitute 5 for  $x$  in  $g$

$$\begin{aligned} g(5) &= 3(2 \times 5 + 1) \\ &= 3(11) = 33 \end{aligned}$$

$$\frac{33 \checkmark}{(1)}$$

(b) Find  $gf(9)$

$$f(x) = \frac{12}{\sqrt{x}} \quad g(x) = 3(2x+1)$$

$g(f(9))$

$$f(9) = \frac{12}{\sqrt{9}} = \frac{12}{3} = 4 \checkmark$$

$$\begin{aligned} g(f(9)) &= g(4) = 3(2 \times 4 + 1) \\ &= 27 \end{aligned}$$

$$\frac{27 \checkmark}{(2)}$$

(c) Find  $g^{-1}(6)$

$$g(x) = 3(2x+1)$$

① finding  $g^{-1}(x)$

$$\begin{aligned} &\rightarrow x = 3(2y+1) \quad (\text{rearrange for } y) \\ \div 3 \downarrow & \frac{x}{3} = 2y+1 \quad \downarrow \div 3 \\ -1 \downarrow & \frac{x}{3} - 1 = 2y \quad \downarrow -1 \\ \div 2 \downarrow & y = \frac{1}{2} \left( \frac{x}{3} - 1 \right) \quad \downarrow \div 2 \\ \therefore g^{-1}(x) &= \frac{1}{2} \left( \frac{x}{3} - 1 \right) \quad \checkmark \end{aligned}$$

$$\begin{aligned} g^{-1}(6) &= \frac{1}{2} \left( \frac{6}{3} - 1 \right) \\ &= \frac{1}{2} \times 1 = \frac{1}{2} \\ & \frac{1}{2} \checkmark \end{aligned}$$

(Total for Question 19 is 5 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



20 Show that  $\frac{\sqrt{180} - 2\sqrt{5}}{5\sqrt{5} - 5}$  can be written in the form  $a + \frac{\sqrt{5}}{b}$  where  $a$  and  $b$  are integers.

$$\begin{aligned}
 \sqrt{180} &= \sqrt{9 \times 20} & \frac{a}{b-c} &= \frac{a(b+c)}{(b-c)(b+c)} & \sqrt{ab} &= \sqrt{a} \times \sqrt{b} \\
 &= \sqrt{9} \times \sqrt{20} & & \frac{b^2 - c^2}{b^2 - c^2} & & \\
 &= 3 \times \sqrt{20} & & & & \\
 &= 3 \times \sqrt{4 \times 5} & & \frac{6\sqrt{5} - 2\sqrt{5}}{5\sqrt{5} - 5} &= & \frac{4\sqrt{5}}{5\sqrt{5} - 5} \\
 &= 3 \times \sqrt{4} \times \sqrt{5} & & & & \\
 &= 3 \times 2 \times \sqrt{5} & & & & = \frac{4\sqrt{5} (5\sqrt{5} + 5)}{(5\sqrt{5} - 5)(5\sqrt{5} + 5)} \quad \checkmark 2 \\
 &= 6\sqrt{5} \quad \checkmark 1 & & & &
 \end{aligned}$$

$$\frac{a}{b+c} = \frac{a}{b} + \frac{a}{c}$$

$$\begin{aligned}
 \therefore a &= 1 \\
 b &= 5
 \end{aligned}$$

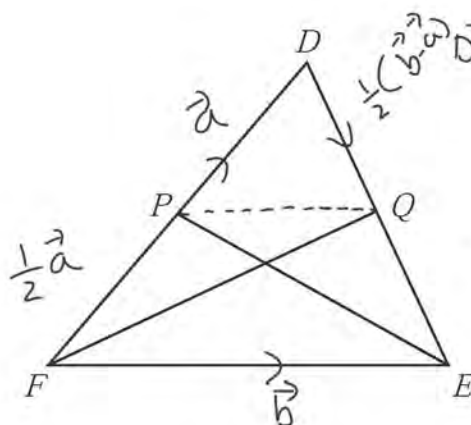
$$\begin{aligned}
 &= \frac{100 + 20\sqrt{5}}{125 - 25} \\
 &= \frac{100 + 20\sqrt{5}}{100} \quad \checkmark 3
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{100}{100} + \frac{20\sqrt{5}}{100} \\
 &= 1 + \frac{\sqrt{5}}{5} \quad \checkmark 4
 \end{aligned}$$

(Total for Question 20 is 4 marks)



21  $DEF$  is a triangle.



$P$  is the midpoint of  $FD$ .

$Q$  is the midpoint of  $DE$ .

$\vec{FD} = \mathbf{a}$  and  $\vec{FE} = \mathbf{b}$

Use a vector method to prove that  $PQ$  is parallel to  $FE$ .

$$\begin{aligned} \vec{DE} &= \vec{DF} + \vec{FE} \\ &= -\vec{a} + \vec{b} \\ &= \vec{b} - \vec{a} \end{aligned}$$

$$\begin{aligned} \vec{DQ} &= \frac{1}{2} \vec{DE} \\ &= \frac{1}{2} (\vec{b} - \vec{a}) \quad \checkmark \end{aligned}$$

$$\begin{aligned} \vec{PQ} &= \vec{PD} + \vec{DQ} \\ &= \frac{1}{2} \vec{a} + \frac{1}{2} (\vec{b} - \vec{a}) \quad \checkmark \end{aligned}$$

$$\begin{aligned} &= \frac{1}{2} \vec{a} + \frac{1}{2} \vec{b} - \frac{1}{2} \vec{a} \\ &= \frac{1}{2} \vec{b} \quad \checkmark \end{aligned}$$

for 2 vectors to be parallel, they must be scalar multiples of each other.

$$\vec{PQ} = \frac{1}{2} \vec{b} \quad \text{and} \quad \vec{FE} = \vec{b}$$

$$\vec{PQ} = \frac{1}{2} \vec{FE} \quad \text{and so} \quad \vec{PQ} \text{ is a scalar multiple of } \vec{FE}.$$

Therefore,  $\vec{PQ}$  and  $\vec{FE}$  are parallel, as required.  $\checkmark$

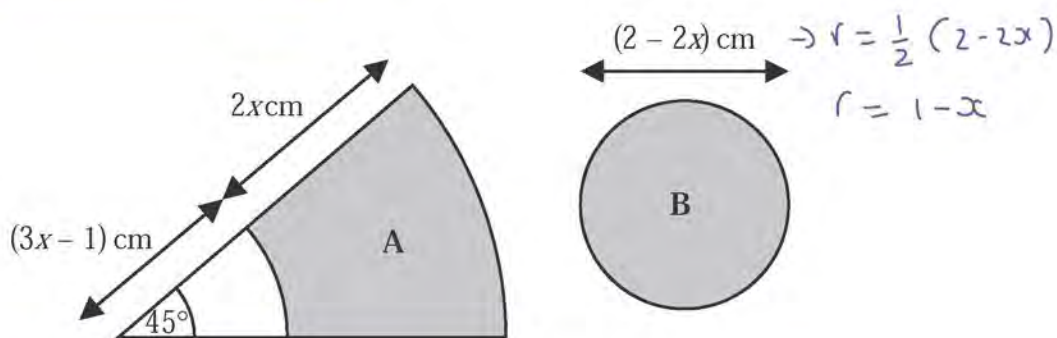
(Total for Question 21 is 4 marks)



22 The diagram shows two shaded shapes, A and B.

Shape A is formed by removing a sector of a circle with radius  $(3x - 1)$  cm from a sector of the circle with radius  $(5x - 1)$  cm.

Shape B is a circle of diameter  $(2 - 2x)$  cm.



The area of shape A is equal to the area of shape B.

Find the value of  $x$ .

You must show all your working.

$$a.o.s = \frac{\theta}{360} \times \pi r^2$$

Area of shape A = area of sector - cutout.

$$\begin{aligned} \text{area of sector} &= \frac{45^\circ}{360^\circ} \times \pi \times (5x - 1)^2 \text{ cm}^2 \\ &= \frac{1}{8} \times \pi \times (5x - 1)^2 \end{aligned}$$

$$\begin{aligned} \text{cutout} &= \frac{45^\circ}{360^\circ} \times \pi \times (3x - 1)^2 \text{ cm}^2 \\ &= \frac{1}{8} \times \pi \times (3x - 1)^2 \end{aligned}$$

$$\begin{aligned} &= \frac{1}{8} \pi \left( (5x - 1)^2 - (3x - 1)^2 \right) \quad \begin{matrix} (5x-1)(5x-1) \\ 25x^2 - 5x - 5x + 1 \end{matrix} \\ &= \frac{1}{8} \pi \left( (25x^2 - 10x + 1) - (9x^2 - 6x + 1) \right) \quad \begin{matrix} (3x-1)(3x-1) \\ 9x^2 - 3x - 3x + 1 \end{matrix} \\ &= \frac{1}{8} \pi (16x^2 - 4x) \quad \begin{matrix} (1-x)(1-x) \\ 1 - x - x + x^2 \end{matrix} \end{aligned}$$

$$\text{area of B} = \pi(1-x)^2 = \pi(x^2 - 2x + 1)$$

$$\begin{aligned} x_1, x_2 &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-2 \pm \sqrt{3^2 - 4(2)(-2)}}{2+2} \\ &= \frac{1}{2}, -2 \quad \checkmark \end{aligned}$$

$$\begin{aligned} \frac{1}{8} (16x^2 - 4x) \pi &= \pi(x^2 - 2x + 1) \\ 16x^2 - 4x &= 8x^2 - 16x + 8 \\ 8x^2 + 12x - 8 &= 0 \\ 2x^2 + 3x - 2 &= 0 \quad \checkmark \end{aligned}$$

(Total for Question 22 is 5 marks)

DO NOT WRITE IN THIS AREA

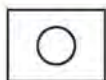
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



23 There are four types of cards in a game.

Each card has a black circle or a white circle or a black triangle or a white triangle.



$$\begin{array}{l} \text{number of cards} \\ \text{with a black shape} \end{array} : \begin{array}{l} \text{number of cards} \\ \text{with a white shape} \end{array} = 3:5$$

$$\begin{array}{l} \text{number of cards} \\ \text{with a circle} \end{array} : \begin{array}{l} \text{number of cards} \\ \text{with a triangle} \end{array} = 2:7$$

Express the total number of cards with a black shape as a fraction of the total number of cards with a triangle.

$$\hookrightarrow \frac{\text{b-shape}}{\text{triangle}} = \frac{3/8 \checkmark_2}{7/9} = \frac{3}{8} \times \frac{9}{7} = \frac{27}{56}$$

$$1/ \text{ fraction for b-shapes} = \frac{3}{8} \checkmark_1 \quad 2/ \text{ fraction for triangle} = \frac{7}{9}$$

$$\frac{27}{56} \checkmark_3$$

(Total for Question 23 is 3 marks)

TOTAL FOR PAPER IS 80 MARKS

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

